CSCI 104
List ADT & Array-based Implementations
Queues and Stacks

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Lists

• Ordered collection of items, which may contain duplicate values, usually accessed based on their position (index)
  – Ordered = Each item has an index and there is a front and back (start and end)
  – Duplicates allowed (i.e. in a list of integers, the value 0 could appear multiple times)
  – Accessed based on their position (list[0], list[1], etc.)

• What are some operations you perform on a list?
List Operations

<table>
<thead>
<tr>
<th>Operation</th>
<th>Description</th>
<th>Input(s)</th>
<th>Output(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>insert</td>
<td>Add a new value at a particular location shifting others back</td>
<td>Index : int Value</td>
<td></td>
</tr>
<tr>
<td>remove</td>
<td>Remove value at the given location</td>
<td>Index : int</td>
<td>Value at location</td>
</tr>
<tr>
<td>get / at</td>
<td>Get value at given location</td>
<td>Index : int</td>
<td>Value at location</td>
</tr>
<tr>
<td>set</td>
<td>Changes the value at a given location</td>
<td>Index : int Value</td>
<td></td>
</tr>
<tr>
<td>empty</td>
<td>Returns true if there are no values in the list</td>
<td></td>
<td>bool</td>
</tr>
<tr>
<td>size</td>
<td>Returns the number of values in the list</td>
<td></td>
<td>int</td>
</tr>
<tr>
<td>push_back / append</td>
<td>Add a new value to the end of the list</td>
<td>Value</td>
<td></td>
</tr>
<tr>
<td>find</td>
<td>Return the location of a given value</td>
<td>Value</td>
<td>Int : Index</td>
</tr>
</tbody>
</table>
IMPLEMENTATIONS
Implementation Strategies

• Linked List
  – Can grow with user needs

• Bounded Dynamic Array
  – Let user choose initial size but is then fixed

• Unbounded Dynamic Array
  – Can grow with user needs
BOUNDDED DYNAMIC ARRAY STRATEGY
A Bounded Dynamic Array Strategy

- Allocate an array of some user-provided size
- What data members do I need?

- Together, think through the implications of each operation when using a bounded array (what issues could the fact that it is bounded cause)?

```cpp
#ifndef BALISTINT_H
#define BALISTINT_H

class BAListInt {
public:
    BAListInt(unsigned int cap);

    bool empty() const;
    unsigned int size() const;
    void insert(int pos, const int& val);
    bool remove(int pos);
    int& const get(int loc) const;
    int& get(int loc);
    void set(int loc, const int& val);
    void push_back(const int& val);

private:
};
#endif
```

balistint.h
A Bounded Dynamic Array Strategy

• What data members do I need?
  – Pointer to Array
  – Current size
  – Capacity

• Together, think through the implications of each operation when using a static (bounded) array
  – Push_back: Run out of room?
  – Insert: Run out of room, invalid location

```cpp
#ifndef BALISTINT_H
#define BALISTINT_H

class BAListInt {
 public:
  BAListInt(unsigned int cap);

  bool empty() const;
  unsigned int size() const;
  void insert(int pos, const int& val);
  void remove(int pos);
  int const & get(int loc) const;
  int & get(int loc);
  void set(int loc, const int& val);
  void push_back(const int& val);

 private:
  int* data_
  unsigned int size_
  unsigned int cap_
};
#endif
```

balist.h
Implementation

• Implement the following member functions
  – A picture to help write the code

```cpp
BAListInt::BAListInt (unsigned int cap)
{
}

void BAListInt::push_back(const int& val)
{
}

void BAListInt::insert(int loc, const int& val)
{
}
```

balist.h (cont)
• Implement the following member functions
  – A picture to help write the code

```cpp
void BAListInt::remove(int loc) {
}
```

balist.h
Const-ness

- What functions stand out as looking strange?

```cpp
#ifndef BALISTINT_H
#define BALISTINT_H

class BAListInt {
    public:
        BAListInt(unsigned int cap);

        bool empty() const;
        unsigned int size() const;
        void insert(int pos, const int& val);
        bool remove(int pos);

        int& const get(int loc) const;
        int& get(int loc);

        void set(int loc, const int& val);
        void push_back(const int& val);

    private:

};
#endif
```
• What functions stand out as looking strange?
• Two versions of get()
• Why do we need two versions of get?
  – 1. Just read a value in the array w/o changes
  – 2. Get a value w/ intention of changing it

```cpp
#ifndef BALISTINT_H
#define BALISTINT_H

class BAListInt {
  public:
    BAListInt(unsigned int cap);

    bool empty() const;
    unsigned int size() const;
    void insert(int pos, const int& val);
    bool remove(int pos);

    int& const get(int loc) const;
    int& get(int loc);

    void set(int loc, const int& val);
    void push_back(const int& val);

  private:
};
#endif
```
// ---- Recall List Member functions ------
// const version
int& const BAListInt::get(int loc) const
{ return data_[i]; }

// non-const version
int& BAListInt::get(int loc)
{ return data_[i]; }

void BAListInt::insert(int pos, const int& val);

// ---- Now consider this code ------
void f1(const BAListInt& mylist)
{
  // This calls the const version of get
  // w/o the const-version this would not compile
  // since mylist was passed as a const parameter
  cout << mylist.get(0) << endl;
  mylist.insert(0, 57); // won't compile..insert is non-const
}

int main()
{
  BAListInt mylist;
  f1(mylist);
}
Returning References

// ---- Recall List Member functions ------
// const version
int& const BAListInt::get(int loc) const
{ return data_[i]; }

// non-const version
int& BAListInt::get(int loc)
{ return data_[i]; }

void BAListInt::insert(int pos, const int& val);

// ---- Now consider this code ------
void f1(BAListInt& mylist)
{
  // This calls the non-const version of get
  // if you only had the const-version this would not compile
  // since we are trying to modify what the
  // return value is referencing
  mylist.get(0) += 1;  // equiv. mylist.set(mylist.get(0)+1);
  mylist.insert(0, 57);
  // will compile since mylist is non-const
}

int main()
{
  BAListInt mylist;
  f1(mylist);
}

• Moral of the Story: We need both versions of get()
UNBOUNDED DYNAMIC ARRAY STRATEGY
Unbounded Array

- Any bounded array solution runs the risk of running out of room when we insert() or push_back()
- We can create an unbounded array solution where we allocate a whole new, larger array when we try to add a new item to a full array

push_back(21) =>

Old, full array

Allocate new array

Copy over items

Add new item

We can use the strategy of allocating a new array twice the size of the old array.
Activity

• What function implementations need to change if any?

```c++
#ifndef ALISTINT_H
#define ALISTINT_H

class AListInt {
public:
  bool empty() const;
  unsigned int size() const;
  void insert(int loc, const int& val);
  void remove(int loc);
  int& const get(int loc) const;
  int& get(int loc);
  void set(int loc, const int& val);
  void push_back(const T& new_val);
private:

  int* _data;
  unsigned int _size;
  unsigned int _capacity;
};

// implementations here
#endif
```
Activity

• What function implementations need to change if any?

```cpp
#ifndef ALISTINT_H
#define ALISTINT_H

class AListInt {
public:
    bool empty() const;
    unsigned int size() const;
    void insert(int loc, const int& val);
    void remove(int loc);
    int& const get(int loc) const;
    int& get(int loc);
    void set(int loc, const int& val);
    void push_back(const T& new_val);
private:
    void resize(); // increases array size
    int* _data;
    unsigned int _size;
    unsigned int _capacity;
};

// implementations here
#endif
```
A Unbounded Dynamic Array Strategy

- Implement the `push_back` method for an unbounded dynamic array

```cpp
#include "alistint.h"

void AListInt::push_back(const int& val) {
}
```
Specialized Lists

STACKS AND QUEUES
Stacks & Queues

• Lists are good for storing generic sequences of items, but they can be specialized to form other useful structures

• What if we had a List, but we restricted how insertion and removal were done?
  – **Stack** – Only ever insert/remove from one end of the list
  – **Queue** – Only ever insert at one end and remove from the other
First-In, First-Out (FIFOs)

QUEUE ADT
Queue ADT

• Queue – A list of items where insertion only occurs at the back of the list and removal only occurs at the front of the list
  – Like waiting in line for a cashier at a store
• Queues are FIFO (First In, First Out)
  – Items at the back of the queue are the newest
  – Items at the front of the queue are the oldest
  – Elements are processed in the order they arrive
A Queue Visual

Items leave from the front
(pop_front)

Items enter at the back
(push_back)
Queue Operations

• What member functions does a Queue have?
  – push_back(item) – Add an item to the back of the Queue
  – pop_front() - Remove the front item from the Queue
  – front() - Get a reference to the front item of the Queue (don't remove it though!)
  – size() - Number of items in the Queue
  – empty() - Check if the Queue is empty
A Queue Class

• A sample class interface for a Queue

• Queue Error Conditions
  – **Queue Underflow** – The name for the condition where you call pop on an empty Queue
  – **Queue Overflow** – The name for the condition where you call push on a full Queue (a Queue that can't grow any more)
    • This is only possible for Queues that are backed by a bounded list

```cpp
#ifndef QUEUEINT_H
#define QUEUEINT_H

class QueueInt {
  public:
    QueueInt();
    ~QueueInt();
    int size() const;
    void push_back(const int& value); //enqueue
    void pop_front(); //dequeue
    int const & front() const;
    bool empty() const;
  private:
    // ???
};

#endif
```
Other Queue Details

• How should you implement a Queue?
  – Back it with an ArrayList
  – Back it with a linked list
  – Back it with a vector
  – Inherit from a linked list
  – Which is best?

<table>
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<th>Pop_front</th>
<th>Front()</th>
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<td>ArrayList</td>
<td></td>
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</tr>
<tr>
<td>LinkedList (Singly-linked w/ tail ptr)</td>
<td></td>
<td></td>
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Other Queue Details

• How should you implement a Queue?
  – Back it with an ArrayList
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Queue Applications

• Print Jobs
  – Click “Print” on the computer is much faster than actually printing (build a backlog)
  – Each job is processed in the order it's received (FIFO)
  – Why would you want a print queue rather than a print stack

• Seating customers at a restaurant

• Anything that involves "waiting in line"

• Helpful to decouple producers and consumers
Last-In, First-Out (LIFOs)

STACK ADT
Stack ADT

• Stack: A list of items where insertion and removal only occurs at one end of the list

• Examples:
  – A stack of boxes where you have to move the top one to get to ones farther down
  – A spring-loaded plate dispenser at a buffet
  – A PEZ dispenser
  – Your e-mail inbox

• Stacks are LIFO
  – Newest item at top
  – Oldest item at bottom

(push)  (pop)
Stack Operations

- What member functions does a Stack have?
  - push(item) – Add an item to the top of the Stack
  - pop() - Remove the top item from the Stack
  - top() - Get a reference to the top item on the Stack (don't remove it though!)
  - size() - Get the number of items in the Stack

- What member data does a Stack have?
  - A list of items
  - Top/Last Item Pointer/Index
A Stack Class

• A sample class interface for a Stack
• How should you implement a Stack?
  – Back it with an array
  – Back it with a vector
  – Back it with a linked list
  – Inherit from linked list
  – Which is best?
• Stack Error Conditions
  – Stack Underflow – The name for the condition where you call pop on an empty Stack
  – Stack Overflow – The name for the condition where you call push on a full Stack (a stack that can't grow any more)

```cpp
#ifndef STACKINT_H
#define STACKINT_H

class StackInt {
    public:
        StackInt();
        ~StackInt();
        int size() const;
        bool empty() const;
        void push(const int& value);
        void pop();
        int const & top() const;
    }

#endif
```
Array Based Stack

• A sample class interface for a Stack
• If using an array list, which end should you use as the "top"?
  – Front or back?
• If using a linked list, which end should you use?
  – If you just use a head pointer only?
  – If you have a head and tail pointer?

```cpp
#ifndef STACKINT_H
#define STACKINT_H

class StackInt {
  public:
    StackInt();
    ~StackInt();
    int size() const;
    bool empty() const;
    void push(const int& value);
    void pop();
    int const& top() const;
  private:
    AListInt mylist_; // or LListInt mylist_
};
#endif
```
Stack Examples

• Reverse a string

```cpp
#include <iostream>
#include <string>
#include "stack.h"
using namespace std;

int main()
{
    StackChar s;

    string word;
    cout << "Enter a word: ";
    getline(cin,word);

    for(int i=0; i < word.size(); i++)
        s.push(word.at(i));

    while(!s.empty())
    {
        cout << s.top();
        s.pop();
    }
}
```

Type in: "hello"
Output: "olleh"
Another Stack Example

- Depth First Search (See Graph Traversals later in this semester)
- Use a stack whenever you encounter a decision, just pick and push decision onto stack. If you hit a dead end pop off last decision (retrace steps) and keep trying, etc.
  - Strait or Left
    - Choose straight...dead end
    - Pop straight and make next choice...left
      - Straight or Right...etc.

http://www.pbs.org/wgbh/nova/einstein/images/lrk-maze.gif
Stack Usage Example

• Check whether an expression is properly parenthesized with '(', '[', '{', '}', ']', ')'
  – Correct: (7 * [8 + [9/{5-2}]]))
  – Incorrect: (7*8
  – Incorrect: (7*8]

• Note: The last parentheses started should be the first one completed

• Approach
  – Scan character by character of the expression string
  – Each time you hit an open-paren: '(', '[', '{' push it on the stack
  – When you encounter a ')', ']', '}' the top character on the stack should be the matching opening paren type, otherwise ERROR!

(7 * [8 + [9/{5-2}]]))

(7 * [4 + 2 + 3])
Double-ended Queues

DEQUE ADT
The Deque ADT

- **Double-ended queues**
- Equally good at pushing and popping on either end

(push_front)  
(pop_front)  
(push_back)  
(pop_back)
STL Deque Class

- Similar to vector but allows for `push_front()` and `pop_front()` options
- Useful when we want to put things in one end of the list and take them out of the other

```cpp
#include <iostream>
#include <deque>
using namespace std;

int main()
{
    deque<int> my_deq;
    for(int i=0; i < 5; i++){
        my_deq.push_back(i+50);
    }
    cout << "At index 2 is: " << my_deq[2] ;
    cout << endl;
    for(int i=0; i < 5; i++){
        int x = my_deq.front();
        my_deq.push_back(x+10);
        my_deq.pop_front();
    }
    while(!my_deq.empty()){
        cout << my_deq.front() << " ";
        my_deq.pop_front();
    }
    cout << endl;
}
```
STL Vector vs. Deque

• **std::vector** is essentially a Dynamic Array List
  – Slow at removing and inserting at the front or middle
  – Fast at adding/remove from the back
  – Implies it could be used well as a (stack / queue)

• **std::deque** gives fast insertion and removal from front and back along with fast random access (i.e. at(i))
  – Almost has "look and feel" of linked list with head and tail pointers providing fast addition/removal from either end
  – Implies it could be used well as a (stack / queue)
  – Practically it is likely implemented as a circular array buffer
Circular Buffers

- Take an array but imagine it wrapping into a circle to implement a deque
- Setup a head and tail pointer
  - Head points at first occupied item, tail at first free location
  - Push_front() and pop_front() update the head pointer
  - Push_back() and pop_back() update the tail pointer
- To overcome discontinuity from index 0 to MAX-1, use modulo operation
  - Index = 7; Index++ should cause index = 0
  - index = (index + 1)%MAX
  - Index = 0; Index-- should cause index = 7
  - if(--index < 0) index = MAX-1;
- Get item at index i
  - It's relative to the head pointer
  - Return item at (head + i)%MAX