

# CS 103 Unit 15

Doubly-Linked Lists and Deques

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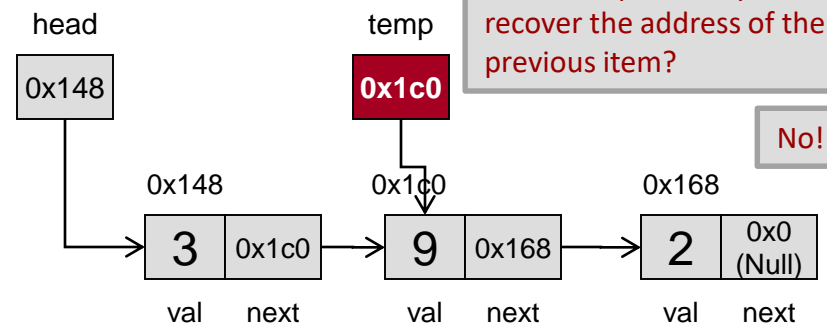
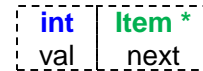
# Singly-Linked List Review

- Used structures/classes and pointers to make 'linked' data structures
- Singly-Linked Lists dynamically allocates each item when the user decides to add it.
- Each item includes a 'next' pointer holding the address of the following Item object
- **Traversal and iteration is only easily achieved in one direction**

```
#include<iostream>
using namespace std;
struct Item {
    int val;
    Item* next;
};

class List
{
public:
    List();
    ~List();
    void push_back(int v); ...
private:
    Item* head;
};
```

struct Item blueprint:



Given temp...could you ever recover the address of the previous item?

No!!!

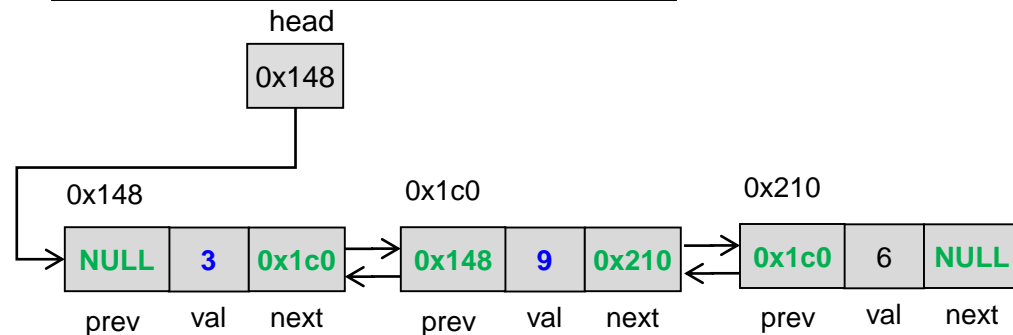
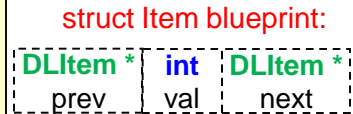
# Doubly-Linked Lists

- Includes a previous pointer in each item so that we can traverse/iterate backwards or forward
- First item's previous field should be NULL
- Last item's next field should be NULL

```
#include<iostream>

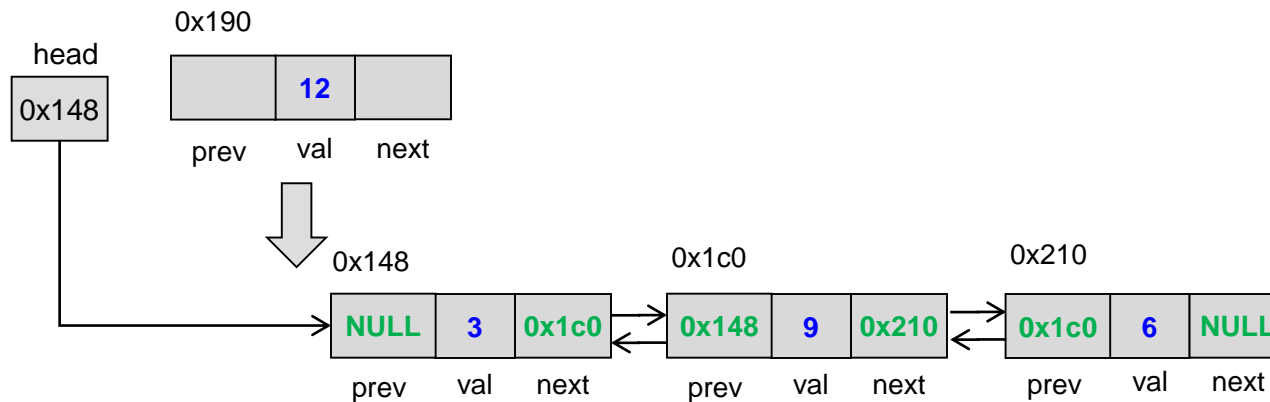
using namespace std;
struct DListItem {
    int val;
    DListItem* prev;
    DListItem* next;
};

class DLList
{
public:
    DLList();
    ~DLList();
    void push_back(int v); ...
private:
    DListItem* head;
};
```



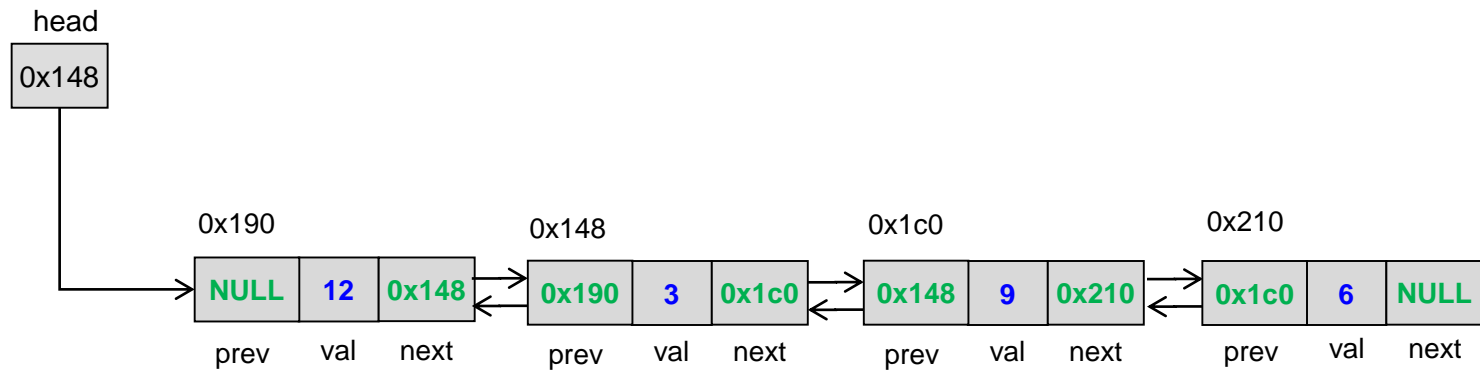
# Doubly-Linked List Add Front

- Adding to the front requires you to update...
- ...Answer
  - Head
  - New front's next & previous
  - Old front's previous



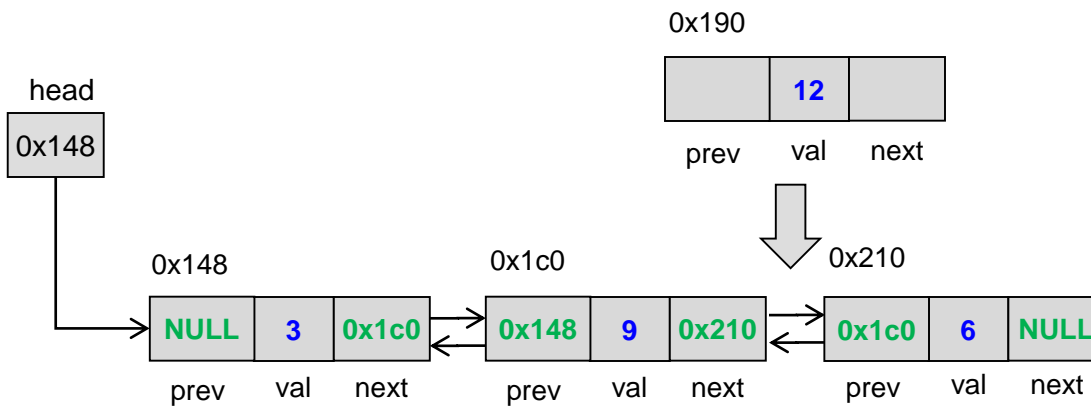
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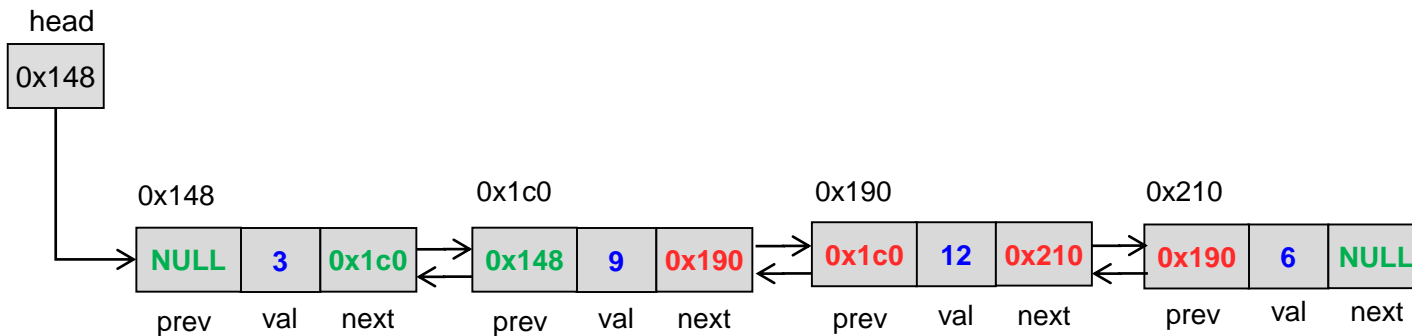
# Doubly-Linked List Add Middle

- Adding to the middle requires you to update...
  - Previous item's next field
  - Next item's previous field
  - New item's next field
  - New item's previous field



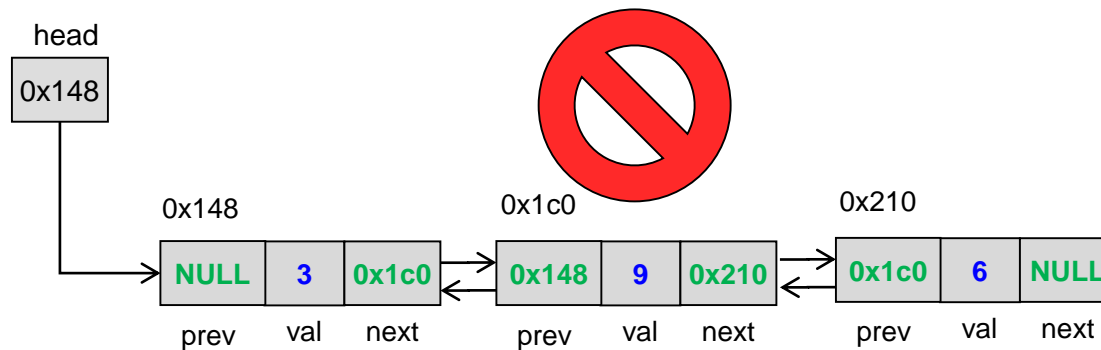
# Doubly-Linked List Add Middle

- Adding to the middle requires you to update...
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# Doubly-Linked List Remove Middle

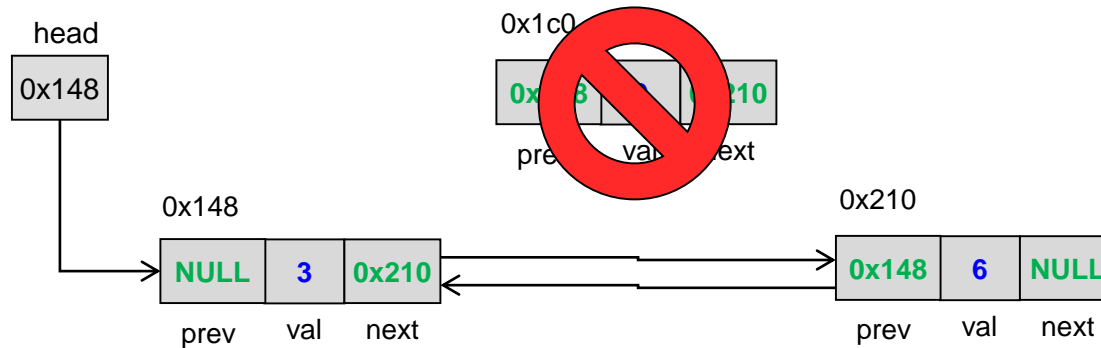
- Removing from the middle requires you to update...
  - Previous item's next field
  - Next item's previous field
  - Delete the item object





# Doubly-Linked List Remove Middle

- Removing from the middle requires you to update...
  - Previous item's next field
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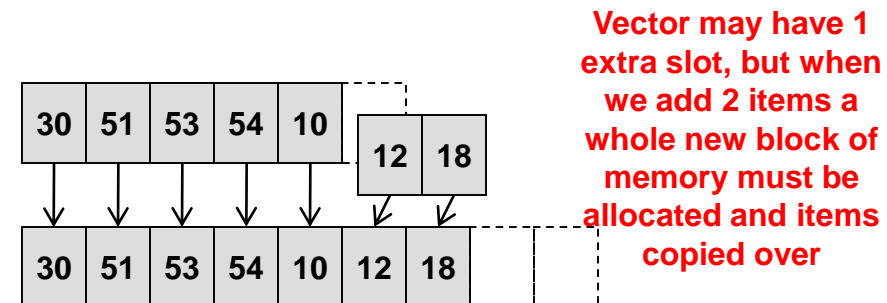
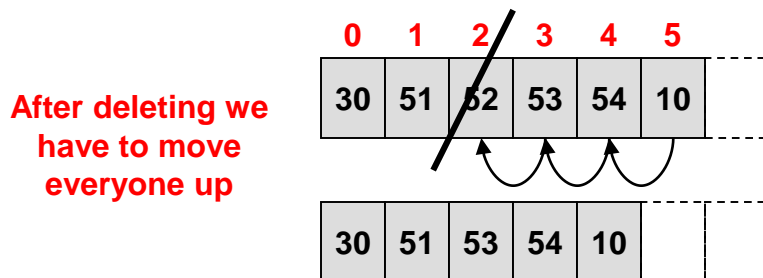


Using a Doubly-Linked List to Implement a Deque

# DEQUES AND THEIR IMPLEMENTATION

# Understanding Performance

- Recall vectors are good at some things and worse at others in terms of performance
- The Good:
  - Fast access for random access (i.e. indexed access such as `myvec[6]`)
  - Allows for ‘fast’ addition or removal of items at the **back** of the vector
- The Bad:
  - Erasing / removing item at the front or in the middle (it will have to copy all items behind the removed item to the previous slot)
  - Adding too many items (vector allocates more memory than needed to be used for additional `push_back()`'s...but when you exceed that size it will be forced to allocate a whole new block of memory and copy over every item)

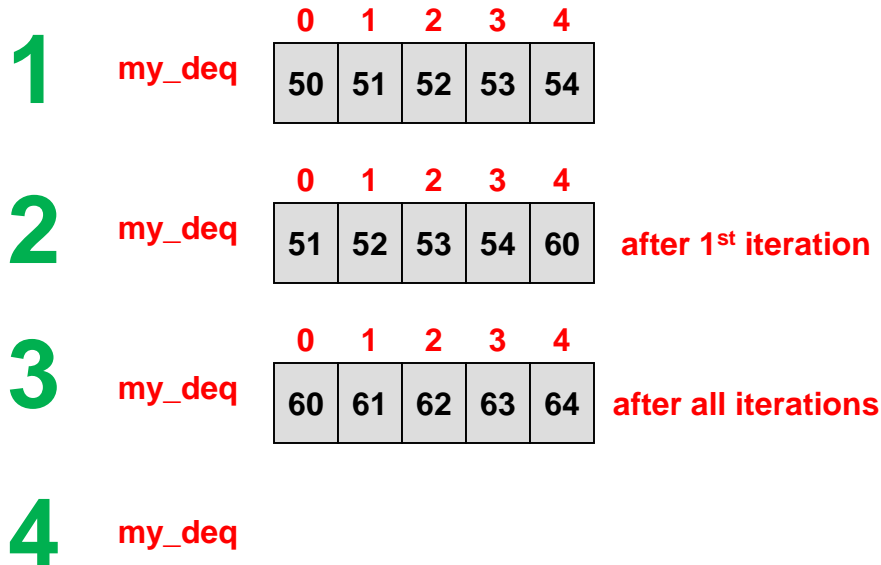


# Deque Class

- Double-ended queues (like their name sounds) allow for efficient (fast) additions and removals from either 'end' (*front or back*) of the list/queue
- Performance:
  - Slightly slower at random access (i.e. array style indexing access such as: `data[3]`) than vector
  - Fast at adding or removing items at *front* or *back*

# Deque Class

- Similar to vector but allows for push\_front() and pop\_front() options
- Useful when we want to put things in one end of the list and take them out of the other



```

#include <iostream>
#include <deque>

using namespace std;

int main()
{
    deque<int> my_deq;
    for(int i=0; i < 5; i++){
        my_deq.push_back(i+50);
    }
    cout << "At index 2 is: " << my_deq[2] ;
    cout << endl;

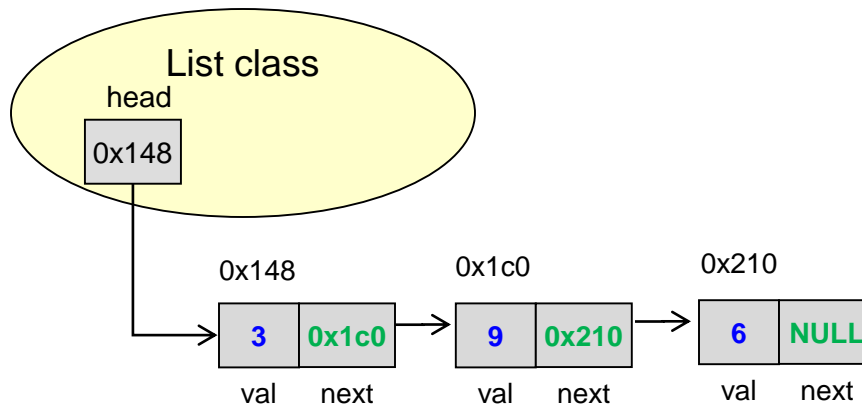
    for(int i=0; i < 5; i++){
        int x = my_deq.front();
        my_deq.push_back(x+10);
        my_deq.pop_front();
    }
    while( ! my_deq.empty()){
        cout << my_deq.front() << " ";
        my_deq.pop_front();
    }
    cout << endl;
}
    
```

# Deque Implementation

- Let's consider how we can implement a deque
- Could we use a singly-linked list and still get fast [i.e.  $O(1)$ ] insertion/removal from both front and back?

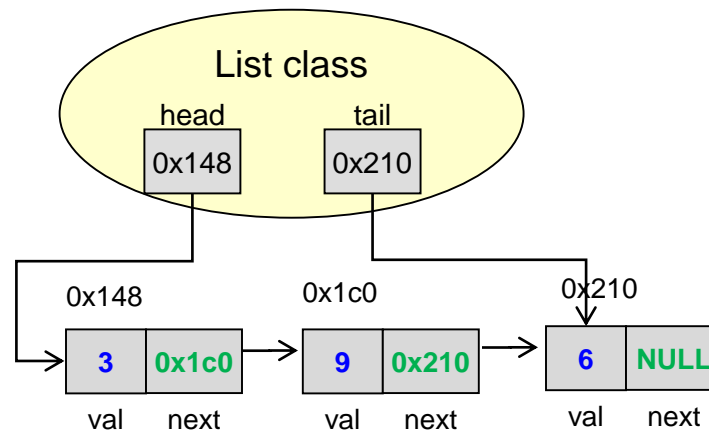
# Singly-Linked List Deque

- Recall a deque should allow for fast [i.e.  $O(1)$ ] addition and removal from front or back
- In our current singly-linked list we only know where the front is and would have to traverse the list to find the end (tail)



# Option 1: Singly-Linked List + Tail Pointer

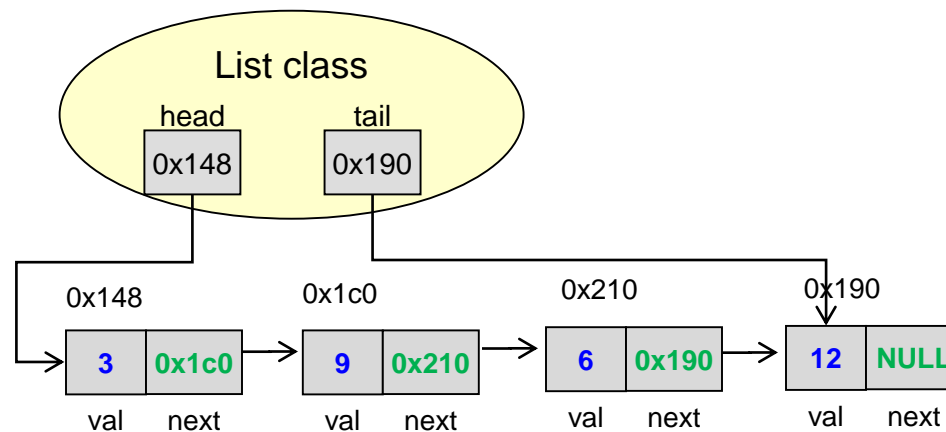
- We might think of adding a tail pointer data member to our list class
  - How fast could we add an item to the end?





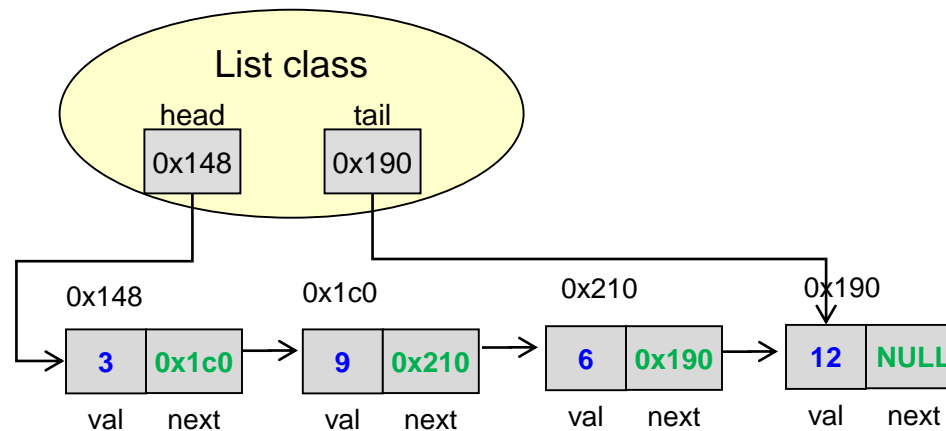
# Option 1: Singly-Linked List + Tail Pointer

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  - How fast could we add an item to the end?  $O(1)$
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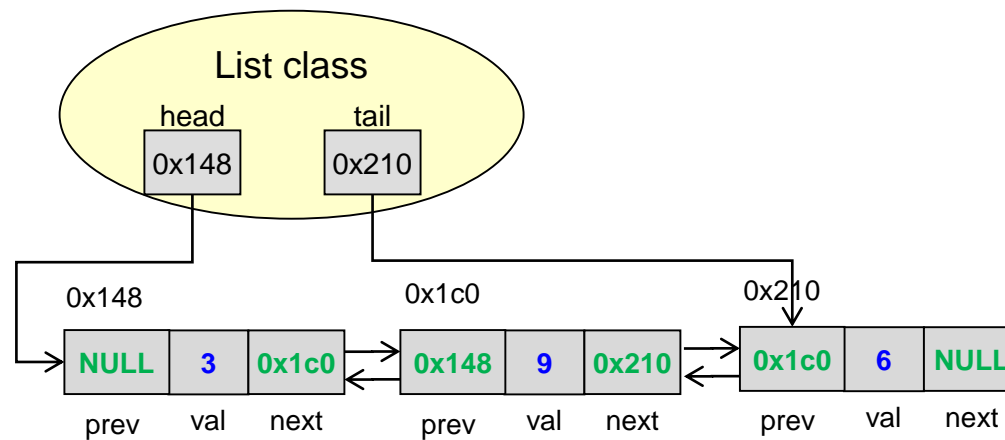
# Option 1: Singly-Linked List + Tail Pointer

- We might think of adding a tail pointer data member to our list class
  - How fast could we add an item to the end?  $O(1)$
  - How fast could we remove the tail item?  $O(n)$ 
    - Would have to walk to the 2<sup>nd</sup> to last item



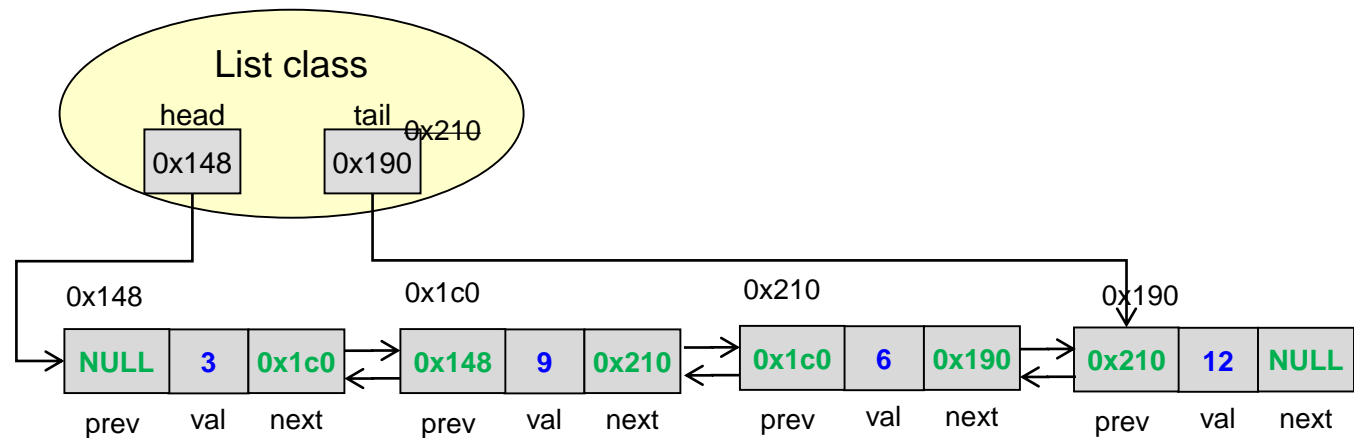
## Option 2: Tail Pointer + Double-Linked List

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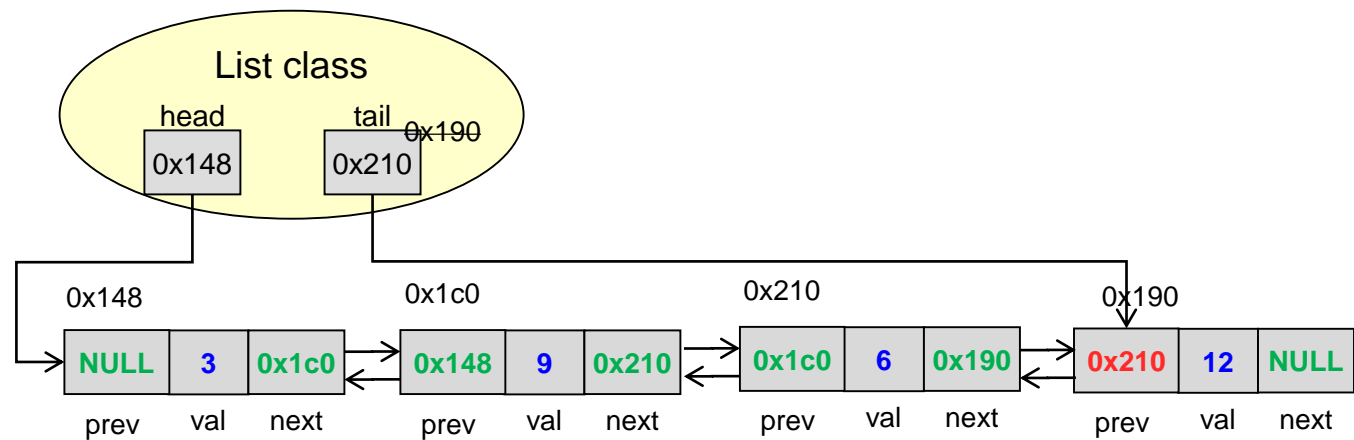
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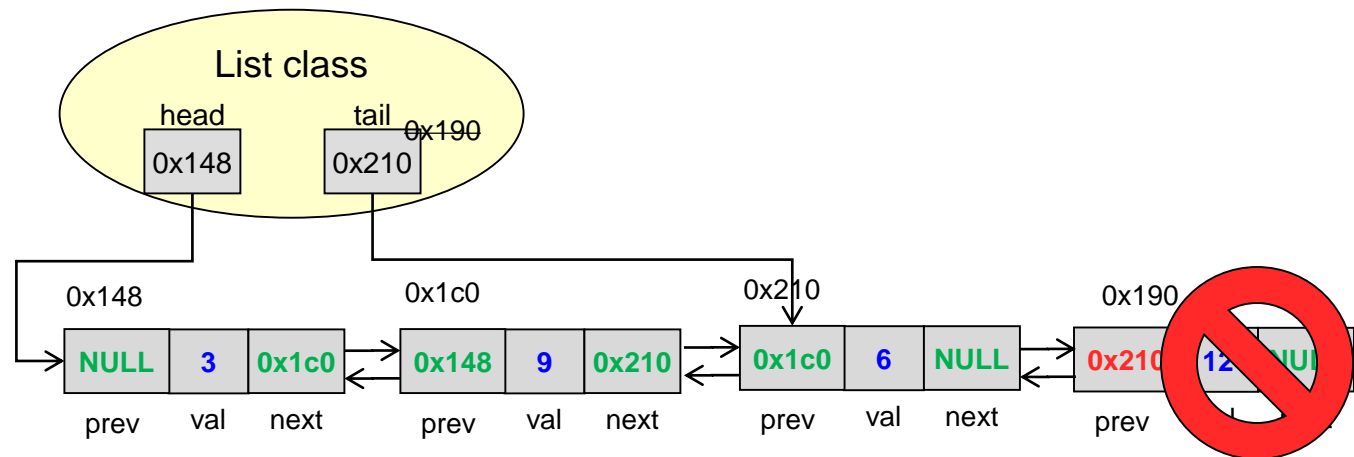
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  - We use the PREVIOUS pointer to update tail



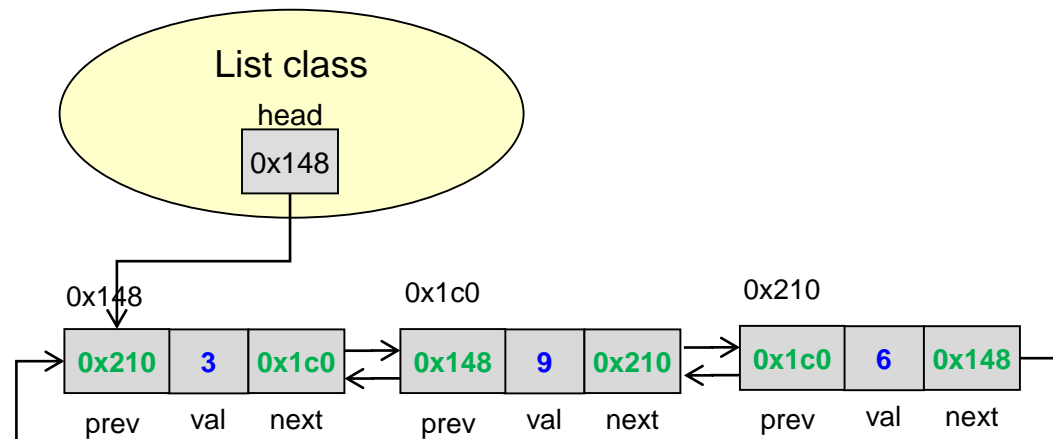
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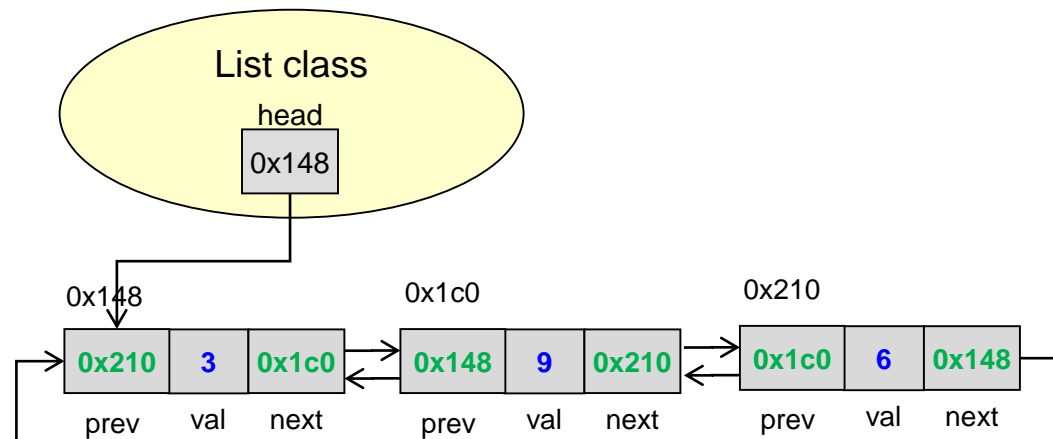
## Option 3: Circular Double-Linked List

- Make first and last item point at each other to form a circular list
  - We know which one is first via the 'head' pointer



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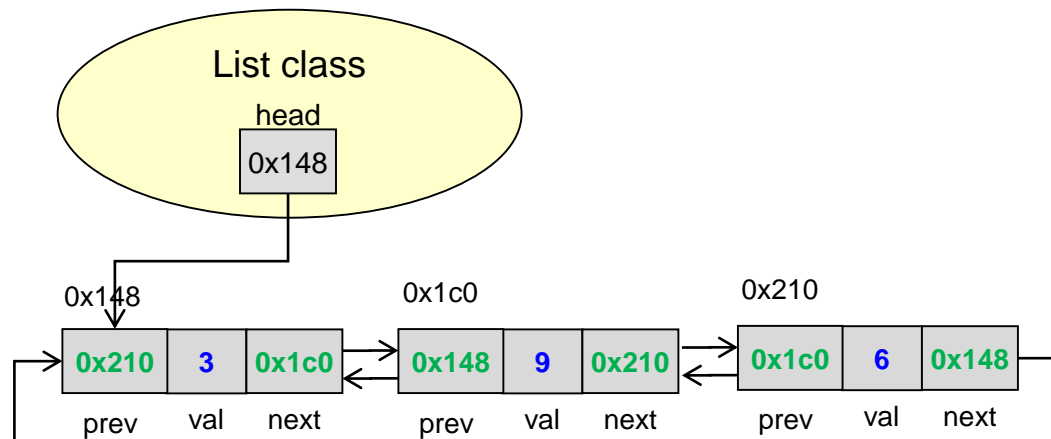
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  - We know which one is first via the 'head' pointer
  - What expression would yield the tail item?





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- Make first and last item point at each other to form a circular list
  - We know which one is first via the 'head' pointer
  - What expression would yield the tail item?
    - head->prev



# One Last Point

- Can this kind of deque implementation support  $O(1)$  access to element  $i$ ?
  - i.e. Can you access `list[i]` quickly for any  $i$ ?
- No!!! Still need to traverse the list
- You can use a "circular" array based deque implementation to get fast random access
  - This is similar to what the actual C++ `deque<T>` class does
  - More to come in CS 104!