Spiral 1 / Unit 7

State Machine Design

Outcomes

- I know the difference between combinational and sequential logic and can name examples of each.
- I understand latency, throughput, and at least 1 technique to improve throughput
- I can identify when I need state vs. a purely combinational function
  - I can convert a simple word problem to a logic function (TT or canonical form) or state diagram
- I can use Karnaugh maps to synthesize combinational functions with several outputs
- I understand how a register with an enable functions & is built
- I can design a working state machine given a state diagram
- I can implement small logic functions with complex CMOS gates

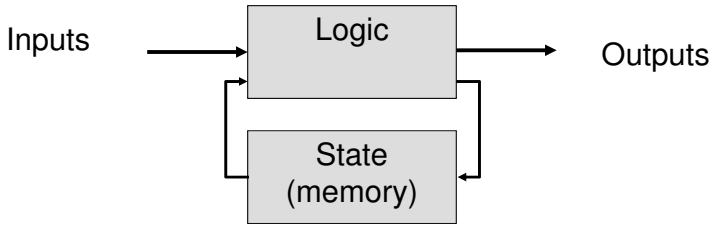
STATE MACHINES OVERVIEW

What is state?

- Decisions are generally influenced by not only what is happening _____, but based on the sum of _____ experiences
  - The sum of all previous experiences is what is known as **state**
- In a human, 'state' refers to the sum of everything that has happened that has led you to where you are now and influences your interpretation of your senses & thoughts
- In a circuit, 'state' refers to all the bits being remembered (_____ or memory)
- In software, 'state' refers to all the _____ values that are being used

State Machine Block Diagram

- A system that utilizes state is often referred to as a state machine (or finite state machine [FSM])
- Most state machines can be embodied in the following form
  - Logic examines what's happening NOW (inputs) & from the PAST (state) to produce outputs and update the state (which will be used in the future to change the decision)
- Inputs will go away or change, so state needs to summarize/capture anything that might be useful for the future

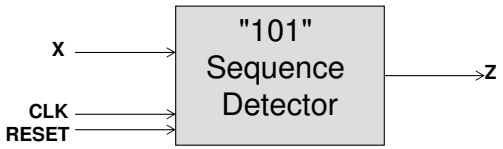


State Machines

- Provide the "brains" or control for electronic and electro-mechanical systems
- Implement a set of steps (or algorithm) to control or solve a problem
- **Goal is to generate output values at _____**
- Combine Sequential and Combinational logic elements
  - Sequential Logic to remember what step (state) we're in
    - Encodes everything that has happened in the past
  - Combinational Logic to produce outputs and find what state to go to next
    - Generates outputs based on what state we're in and the input values
- Use _____ (a.k.a. flowcharts) to specify the operation of the corresponding state machine

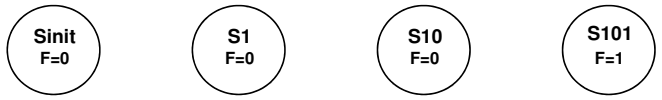
State Machine Example

- Design a sequence detector to check for the combination "101"
- Input, X, provides 1-bit per clock
- Check the sequence of X for "101" in successive clocks
- If "101" detected, output Z=1 (Z=0 all other times)



Another State Diagram Example

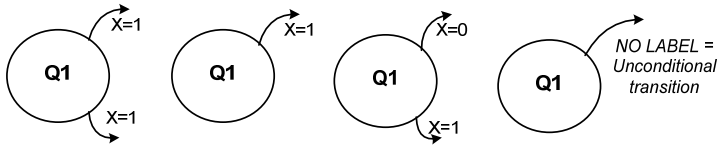
- "101" Sequence Detector should output F=1 when the sequence 101 is found in consecutive order



State Diagram for "101" Sequence Detector

Correct Specification of State Diagrams

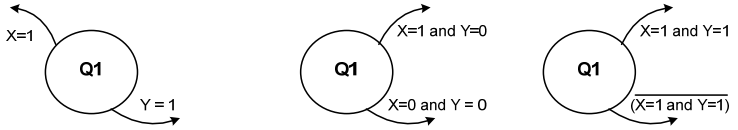
- _____ transition from a state may be true at a time
  - Not 2, not 0, exactly 1
  - Make sure the conditions you associate with the arrows coming out of a state are _____ (< 2 true) but _____ (> 0 true)



Incorrect (2 conditions true) *Incorrect (No condition for X = 0)* *Correct* *Correct*

Correct Specification of State Diagrams 2

- Exactly one transition from a state may be true at a time



Incorrect (More than one condition can be true) *Incorrect (Not all conditions covered)* *Correct (1 and only 1 condition will be true at all times)*

State Machines

- State Machines can be broken into 3 sections of logic
  - State Memory (SM)
    - Just FF's to remember the *current state*
  - Next State Logic (NSL)
    - Combo logic to determine the next state
    - Essentially implements the transition conditions
  - Output Function Logic (OFL)
    - Combo logic to produce the outputs

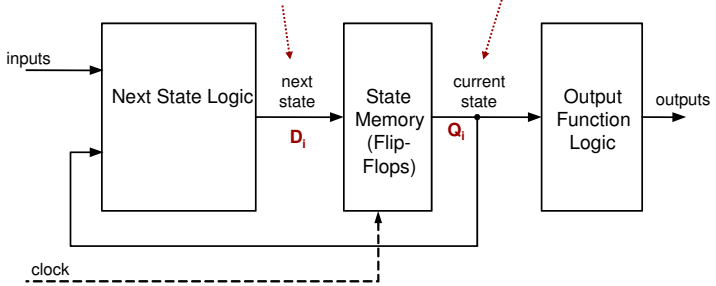
State Machine

NEXT STATE

The FF inputs will be the value of the next state (on the next clock edge the FF outputs will change based on the inputs)

CURRENT STATE

The FF outputs represent the current state (the state we're in right now)



Important: State is always represented and stored by the _____ in the system

State Machine Outputs

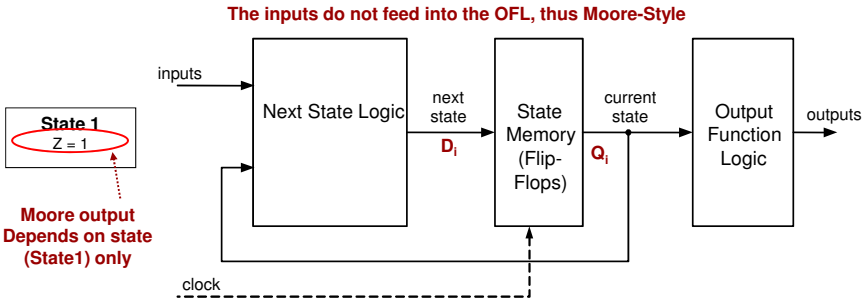
- State Machine outputs can be classified according to how the outputs are produced

  – If *Outputs = f(*_____*)*…
  _____-Style

  – If *Outputs = f(*_____*)*…
  _____-Style

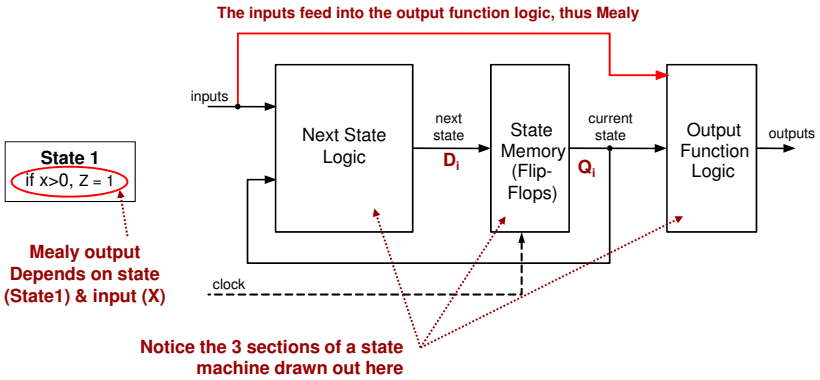
Moore-Style Outputs

- Moore-style outputs only depend on the current state
- Thus, they are valid _____ in the clock cycle and _____ nearly the entire
- Often requires extra states compared to Mealy-style implementations



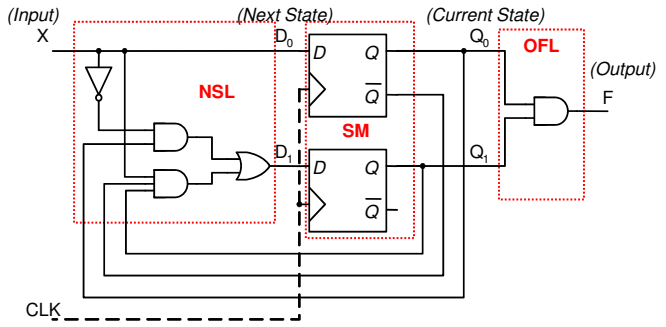
Mealy-Style Outputs

- Mealy-style outputs depend not only on the current state but the external inputs
- Thus, they may not be valid until _____ in the clock cycle and _____ during the cycle if the inputs change



State Machines

- Below is a circuit implementing a state machine, notice how it breaks into the 3 sections



STATE MACHINE DESIGN

State Machine Review

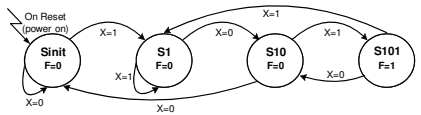
State Diagrams

1. States
2. Transition Conditions
3. Outputs

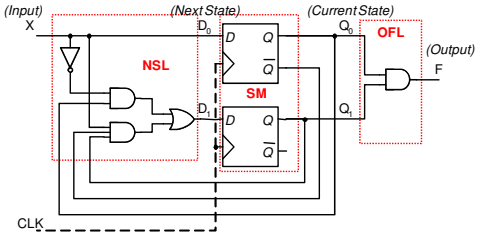
State Machine

1. State Memory => FF's
   - n-FF's => 2^n states
2. Next State Logic (NSL)
   - combinational logic
   - logic for FF inputs
3. Output Function Logic (OFL)
   - MOORE: f(state)
   - MEALY: f(state + inputs)

State Machines require sequential logic to remember the current state (w/ just combo logic we could only look at the current value of X, but now we can take 4 separate actions when X=0)



State Diagram for "101" Sequence Detector



State Machine Design

- State machine design involves taking a problem description and coming up with a state diagram and then designing a circuit to implement that operation

Problem Description → **State Diagram** → **Circuit Implementation**

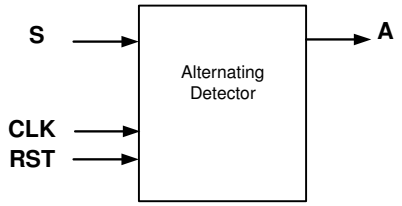
State Machine Design

- Coming up with a state diagram is non-trivial
- Requires creative solutions
- Designing the circuit from the state diagram is done according to a simple set of steps
- To come up w/ a state diagram to solve a problem
  - Write out an algorithm or _____to solve the problem
  - Each step in your algorithm will usually be _____ in your state diagram
  - Ask yourself what past inputs need to be remembered and that will usually lead to a state representation

EXAMPLE 1

Alternating Detector

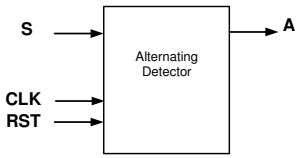
- Given bits coming in from a sensor, design a system that outputs true if sequential bits alternate or false if the same bit value is detected in that past two clock cycles



Alternating Detector Example

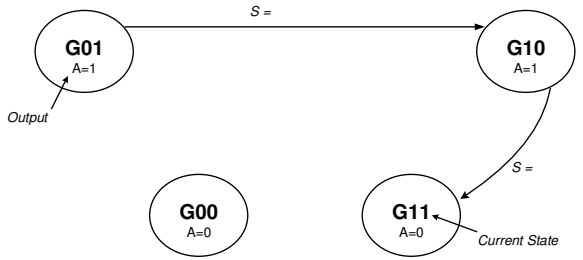
- Can take a Mealy or Moore approach

•Mealy Approach
(usually requires less states):



Alternating Detector

- Design a state machine to check if sensor produces two 0's in a row (i.e. 2 consecutive spaces) or two 1's in a row (i.e. 2 consecutive teeth)



•G10 = Last cycle we got 1, two cycles ago we got 0

•G01 = Last cycle we got 0, two cycles ago we got 1

•G11 = Got 2 consecutive 1's

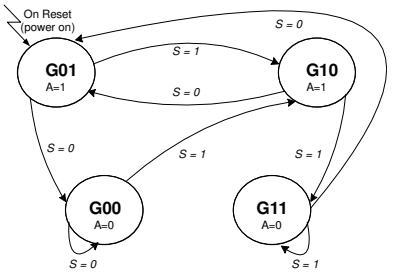
•G00 = Got 2 consecutive 0's

6 Steps of State Machine Design

1. State Diagram
2. Transition/Output Table
3. State Assignment
   - Determine the # of FF's required
   - Assign binary codes to replace symbolic names
4. Excitation Table (Rename Q* to D)
5. K-Maps for NSL and OFL
   - One K-Map for every FF input
   - One K-Map for every output of OFL
6. Draw out the circuit

Transition Output Table

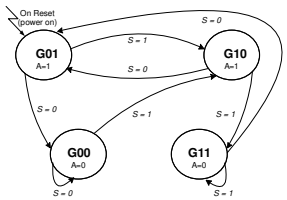
- Convert state diagram to transition/output table
  - Show Next State & Output as a function of Current State and Input



Current State	Input (S)	Next State	Output (A)
G01	0		1
G01	1		1
G11	0		0
G11	1		0
G00	0		0
G00	1		0
G10	0		1
G10	1		1

Transition Output Table

- Now assign binary codes to represent states



State Assignment Mapping

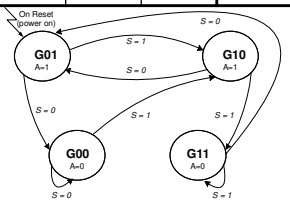
State	Q_1	Q_0
G01	0	0
G11	0	1
G00	1	0
G10	1	1

Current State		Input	Next State		Output
Q1	Q0	S	Q1*	Q0*	A
0	0	0	1	0	1
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	1	0
1	0	0	1	0	0
1	0	1	1	1	0
1	1	0	0	0	1
1	1	1	0	1	1

Transition Output Table

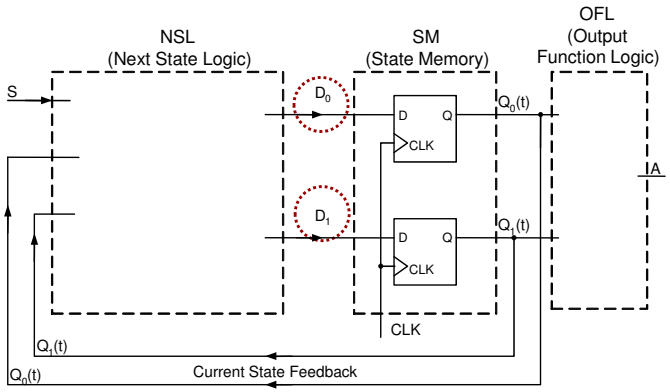
- Convert state diagram to transition/output table

Current State			Next State						Output
			S = 0			S = 1			
State	Q_1	Q_0	State			State			A
G01	0	0	G00			G10			1
G11	0	1	G01			G11			0
G10	1	1	G01			G11			1
G00	1	0	G00			G10			0



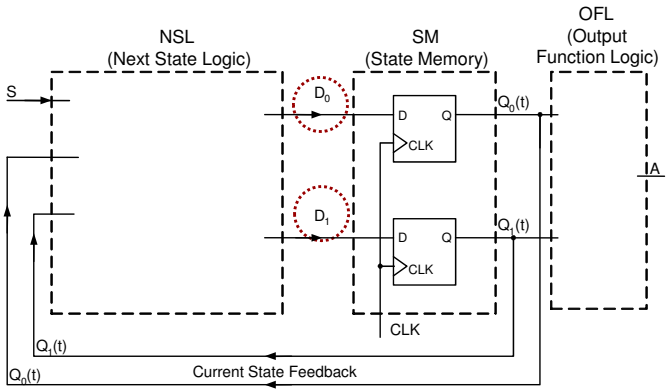
Excitation Table

- The goal is to produce logic for the inputs to the FF's (D_1,D_0)…these are the excitation equations



Excitation Table

- Using your transition table you know what you want Q* to be, but how can you make that happen?
- For D-FF's Q* will be whatever D is at the edge



Excitation Table

- In a D-FF Q* will be whatever D is, so if we know what we want Q* to be just make sure that's what the D input is

Current State			Next State						Output
			S = 0			S = 1			
State	Q_1	Q_0	State	D_1	D_0	State	D_1	D_0	A
G01	0	0	G00	1	0	G10	1	1	1
G11	0	1	G01	0	0	G11	0	1	0
G10	1	1	G01	0	0	G11	0	1	1
G00	1	0	G00	1	0	G10	1	1	0

Karnaugh Maps

- Now need to perform K-Maps for D1, D0, and A

Current State			Next State						Output
			S = 0			S = 1			
State	Q_1	Q_0	State	D_1	D_0	State	D_1	D_0	A
G01	0	0	G00	1	0	G10	1	1	1
G11	0	1	G01	0	0	G11	0	1	0
G10	1	1	G01	0	0	G11	0	1	1
G00	1	0	G00	1	0	G10	1	1	0

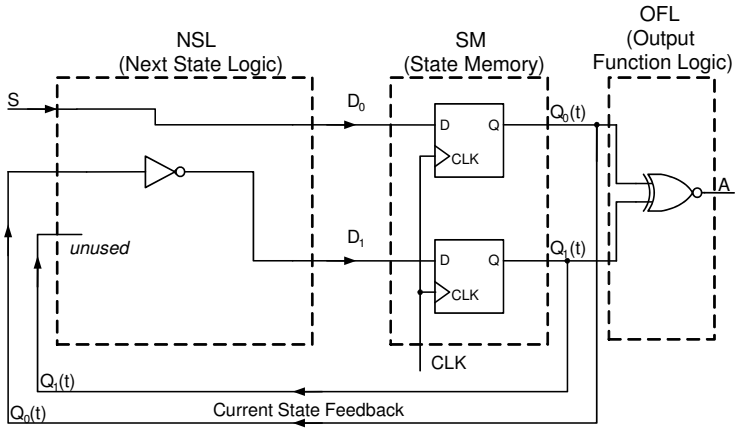
Q1Q0 \ S	0	1
00	1	1
01	0	0
11	0	0
10	1	1

Q1Q0 \ S	0	1
00	0	1
01	0	1
11	0	1
10	0	1

Q0 \ Q1	0	1
0	1	0
1	0	1

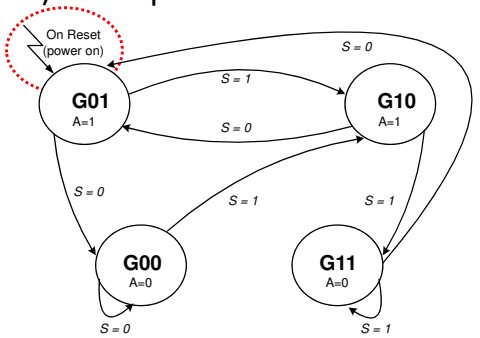
Implementing the Circuit

- Implements the alternating detector



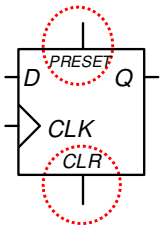
Implementing an Initial State

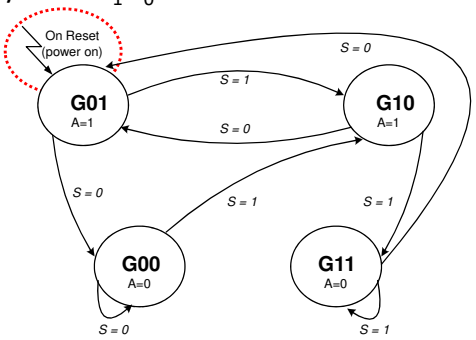
- How can we make the machine start in G0 on reset (or power on?)
- Flip-flops by themselves will initalize to a random state (1 or 0) when power is turned on



Implementing an Initial State

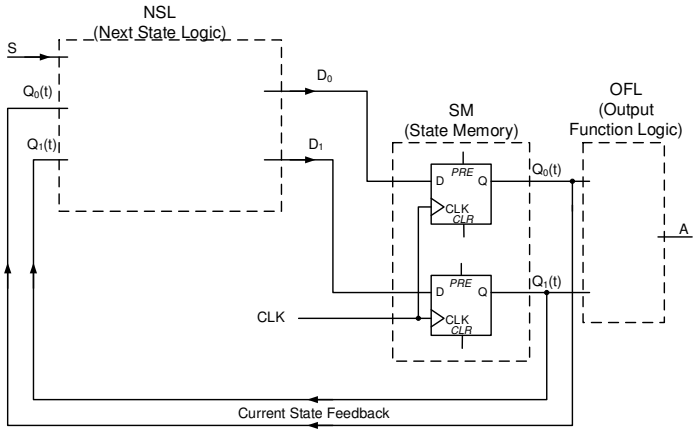
- Use the CLEAR and PRESET inputs on our flip-flops in the state memory
  - When CLEAR is active the FF initializes Q=0
  - When PRESET is active the FF initializes Q=1
- We assigned G0 the binary code Q_1Q_0=00 so we must initialize our Flip-Flop's to 00





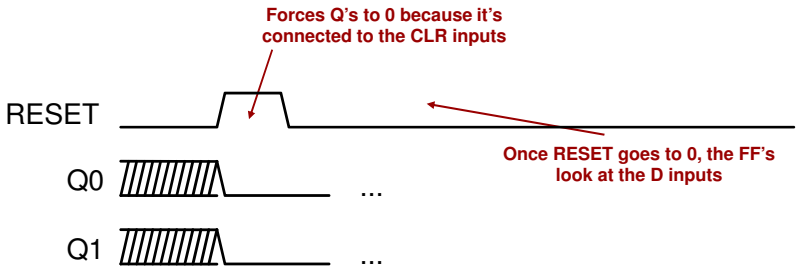
Implementing an Initial State

- Use the CLR inputs of your FF's along with the RESET signal to initialize them to 0's and tie off the PRE inputs



Implementing an Initial State

- When RESET is activated Q's initialize to 0 and then when it goes back to 1 the Q's look at the D inputs



Alternate State Assignment

- **Important Fact**: The _____ **we assign** to our states can have a big impact on the size of the NSL and OFL
- Let us work again with a different set of assignments

State	Q_1	Q_0
G01	0	0
G11	0	1
G10	1	1
G00	1	0

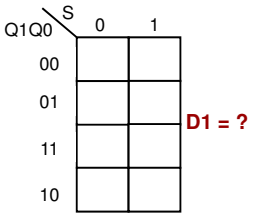
Old Assignments

Current State			Next State						Output
			S = 0			S = 1			
State	Q_1	Q_0	State			State			A
G01	0	0	G00			G10			1
G10	0	1	G01			G11			1
G00	1	1	G00			G10			0
G11	1	0	G01			G11			0

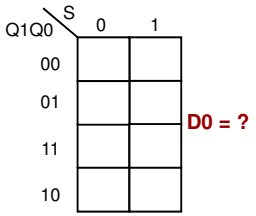
New Assignments

Alternate State Assignment

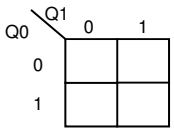
Current State			Next State						Output
			S = 0			S = 1			
State	Q_1	Q_0	State	Q1*= D1	Q0*= D0	State	Q1* =D1	Q0* =D0	A
G01	0	0	G00	1	1	G10	0	1	1
G10	0	1	G01	0	0	G11	1	0	1
G00	1	1	G00	1	1	G10	0	1	0
G11	1	0	G01	0	0	G11	1	0	0



D1 = ?



D0 = ?

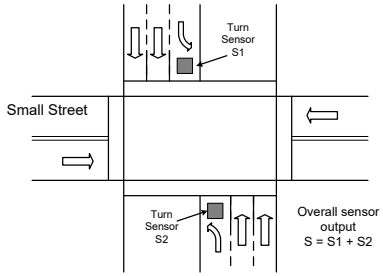


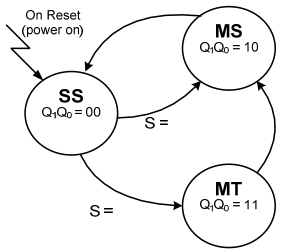
A = ?

EXAMPLE 2

Traffic Light Controller

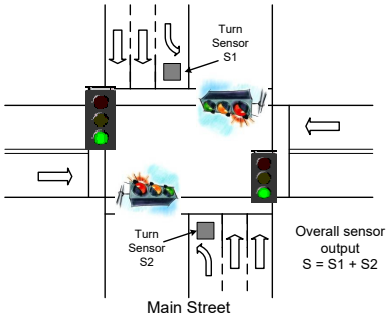
- Design the controller for a traffic light at an intersection
  - Main street has a protected turn while small street does not
    - Sensors embedded in the street to detect cars waiting to turn
    - Let S = _____ to check if any car is waiting
  - Simplify and only have Green and Red lights (no yellow)

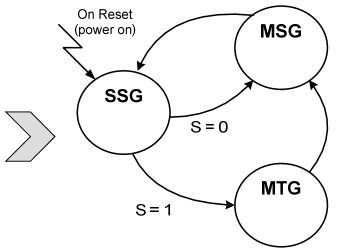




State Assignment

- Design of the traffic light controller with main turn arrow
- Represent states with some binary code
  - Codes: 3 States => 2 bit code: 00=SSG, 10=MSG, 11=MTG



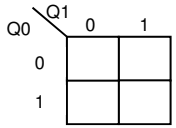


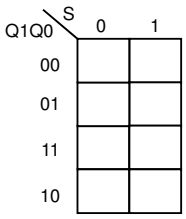
State Diagram

K-Maps

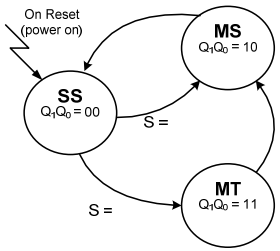
- Find logic for each FF input by using K-Maps

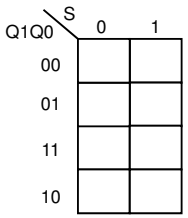
Current State			Next State						Output		
			S = 0			S = 1					
State	Q_1	Q_0	State	Q_1^+	Q_0^+	State	Q_1^+	Q_0^+	SSG	MTG	MSG
SS	0	0									
N/A	0	1									
MT	1	1									
MS	1	0									





$D_1 =$



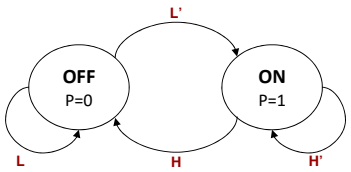


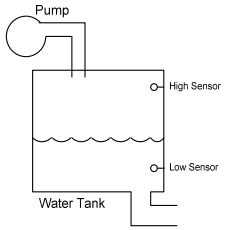
$D_0 =$

EXAMPLE 3

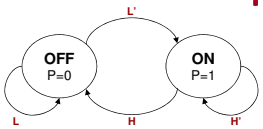
Water Pump

- Implement the water pump controller using the High and Low sensors as inputs





Transition Table



Current State		Next State							
		H L = 0 0		H L = 0 1		H L = 1 1		**H L = 1 0**	
Symbol	Q	Sym.	Q*	Sym.	Q*	Sym.	Q*	Sym.	**Q***
OFF	0								
ON	1								

Note: The State Value, Q forms the Pump output (i.e. 1 when we want the pump to be on and 0 othewise)

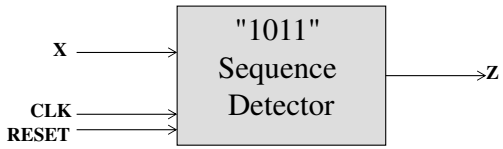
H L \ Q	0	1
00		
01		
11		
10		

D =

EXAMPLE 4

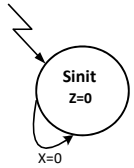
State Machine Example

- Design a sequence detector to check for the combination "1011"
- Input, X, provides 1-bit per clock
- Check the sequence of X for "1011" in successive clocks
- If "1011" detected, output Z=1 (Z=0 all other times)



State Diagram

- Be sure to handle overlapping sequences



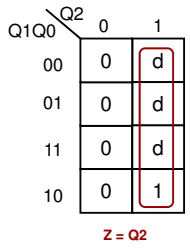
Transition Output Table

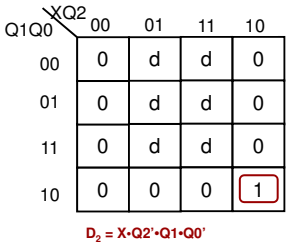
- Translate the state diagram into the transition output table

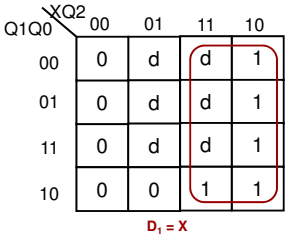
Current State				Next State								Output
				X = 0				X = 1				
State	Q2	Q1	Q0	State*	Q2*	Q1*	Q0*	State*	Q2*	Q1*	Q0*	Z
Sinit	0	0	0									0
S10	0	0	1									0
S1	0	1	1									0
S101	0	1	0									0
S1011	1	1	0									1

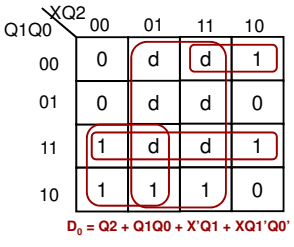
NSL & OFL

Current State				Next State								Output
				X = 0				X = 1				
State	Q2	Q1	Q0	State*	D2	D1	D0	State*	D2	D1	D0	Z
Sinit	0	0	0	Sinit	0	0	0	S1	0	1	1	0
S10	0	0	1	Sinit	0	0	0	S101	0	1	0	0
S1	0	1	1	S10	0	0	1	S1	0	1	1	0
S101	0	1	0	S10	0	0	1	S1011	1	1	0	0
S1011	1	1	0	S10	0	0	1	S1	0	1	1	1

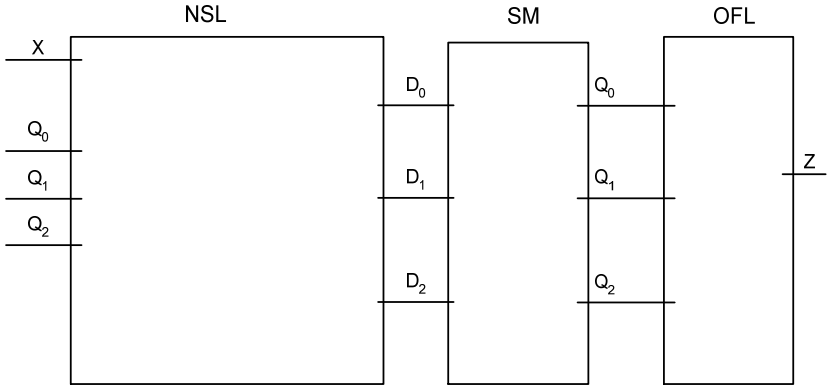








Drawing the Circuit



Waveform for 1011 Detector